## Abstract of the two lectures on Mar 01 and Mar 02, 2019 (at the Department of Mathematics, IIT Bombay)

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Title : Hilbert-Samuel functions

Continuing from the two lectures on Jan 28 and Jan 31, 2019 on S o m e questions on the H i l b e r t - S a m u e l f u n c t i o n s, in these two lectures on Mar 01 and Mar 04, 2019, we prove the Theorem 2 which is more general than the Theorem 1 which was proved in last lectures. More precisely, we prove the following theorem :

**Theorem 2** Let A be a noetherian excellent local ring and  $\mathfrak{p} \in \operatorname{Spec} A$  with  $d := \dim A/\mathfrak{p}$ . Then  $\operatorname{H}_{A_{\mathfrak{p}}}^{(d)} \leq \operatorname{H}_{A}^{(0)}$ .